

HMIC 2025/5

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Twitch Solves ISL

Episode 162

Problem

Compute the smallest integer $k > 45$ for which there exists a sequence $a_1, a_2, a_3, \dots, a_{k-1}$ of positive integers satisfying the following conditions:

- $a_i = i$ for all integers $1 \leq i \leq 45$;
- $a_{k-i} = i$ for all integers $1 \leq i \leq 45$, and
- for any odd integers $1 \leq n \leq k - 45$, the sequence $a_n, a_{n+1}, \dots, a_{n+44}$ is a permutation of $\{1, 2, \dots, 45\}$.

Video

<https://youtu.be/W5rdrCAtB08>

Solution

To be written.