

# SMO 2020/5

Evan Chen

TWITCH SOLVES ISL

Episode 27

## Problem

In triangle  $ABC$ , let  $E$  and  $F$  be points on sides  $AC$  and  $AB$ , respectively, such that  $BFEC$  is cyclic. Let lines  $BE$  and  $CF$  intersect at point  $P$ , and  $M$  and  $N$  be the midpoints of  $\overline{BF}$  and  $\overline{CE}$ , respectively. If  $U$  is the foot of the perpendicular from  $P$  to  $BC$ , and the circumcircles of  $\triangle BMU$  and  $\triangle CNU$  intersect at second point  $V$  different from  $U$ , prove that  $A$ ,  $P$ , and  $V$  are collinear.

## Video

<https://youtu.be/XlXnHk9AtAE>

