

Time limit: 4 hours 30 minutes.
Each problem is worth 7 points.

Error Littered Math Olympiad

Year: 2025



27th ELSMO
AURORA, IL



Day: 1

June 14, 2025
12:30PM-5:00PM CDT

Problem 1. Let $\mathbb{Z}_{>0}$ denote the set of positive integers. Find all functions $f: \mathbb{Z}_{>0} \rightarrow \mathbb{Z}_{>0}$ such that for all positive integers m and n ,

$$f^m(n) + f(mn) = f(m)f(n).$$

Problem 2. A contest has 2025 problems. Elmo initially knows that the answers are $1, 2, \dots, 2025$ in some order. Every minute, Elmo selects a problem that has not been answered correctly, inputs an answer to it, and is told whether the answer is correct or incorrect. Elmo wins the contest if and only if he answers all 2025 problems correctly in at most 2024 attempts each. Can Elmo guarantee that he wins the contest?

Problem 3. Let n be a positive integer and p be a prime. Over all integer-coefficient polynomials $P(x)$ with an x^n coefficient of 1, find the largest power of p that can divide $P(x)$ for all integers x .

*Time limit: 10 minutes.
Each problem is worth 0 points.*

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27th ELSMO
AURORA, IL



Year: 2025

Day: 2

*June 21, 2024
1:20PM-5:50PM EDT*

Problem 4. Find the smallest four-digit positive integer $n = \overline{abcd}_{10}$ with $a \neq 0$, $c \neq 0$ such that $\varphi(n) = \overline{ab}_{10} \cdot \overline{cd}_{10}$, where $\varphi(n)$ is the Euler totient function.

Problem 5. Can every convex decagon be dissected into pentagons, each of which has every angle greater than 90 degrees?

Problem 6. Let Gamma be a circle. Point A is a point on Gamma and point B is a point strictly inside Gamma. The perpendicular bisector of AB intersects Gamma at E and F. Lines BE and BF intersect Gamma again at X and Y. Prove that angle BAX and BAY are equal.

*Time limit: 10 minutes.
Each problem is worth 0 points.*